

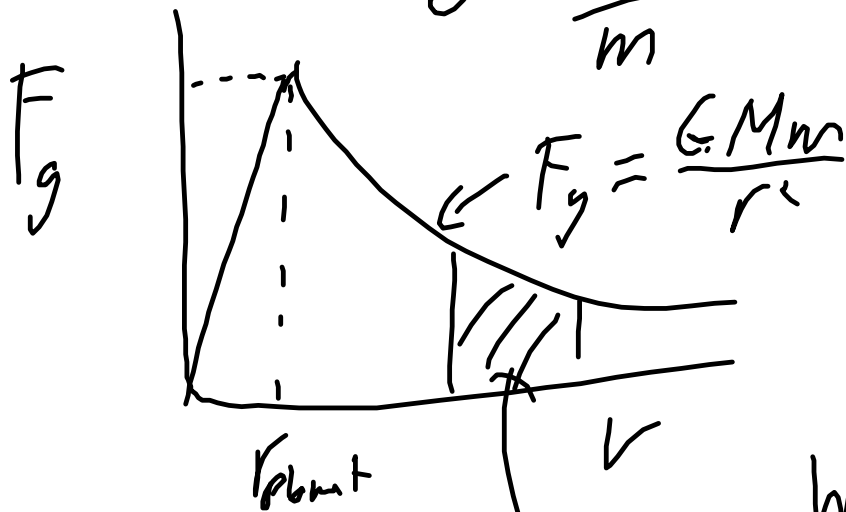
Gravitational Energy

field strength

- Energy of orbital motion
- Energy of interplanetary projectiles

Recall:

$$g = \frac{F_g}{m} = \frac{GM}{r^2}$$



$$\text{Area} = W_g = \Delta E_g$$

$$\int F_g dr = \int \frac{GMm}{r^2} dr = -GMm \left(\frac{1}{r_f} - \frac{1}{r_i} \right)$$

$$\frac{1}{3} - \frac{1}{2} \neq 1$$

$$E_g = -\frac{GMm}{r}$$

relative to

$$E_g \rightarrow 0 \text{ as } r \rightarrow \infty$$

Work done moving mass m from ∞ to r

Graph of E_g , E_k and E_T

- i) mass m in orbit radius r around mass M .
- ii) mass m moving at velocity v away from mass M
 - a) at escape speed
 - b) $v < v_{\text{escape}}$
 - c) $v > v_{\text{escape}}$

- derive an equation for
 $F_g = F_c \rightarrow F_k$ in terms of r, M, m for orbit

- derive escape speed equation

$$\left| \frac{GMm}{r} \right| = \frac{1}{2} m v^2$$

$$v_{\text{escape}} = \sqrt{\frac{2GM}{r}}$$

Don't confuse with $V = -GM/r$

V is gravitational potential defined as the gravitational energy per unit mass.

or, don't confuse with orbital speed

$$F_g = F_c$$

$$\frac{GMm}{r^2} = \frac{\cancel{m}v^2}{\cancel{r}}$$

$$v_{\text{orbit}} = \sqrt{\frac{GM}{r}}$$

orbital kinetic Energy $\rightarrow |E_g|$

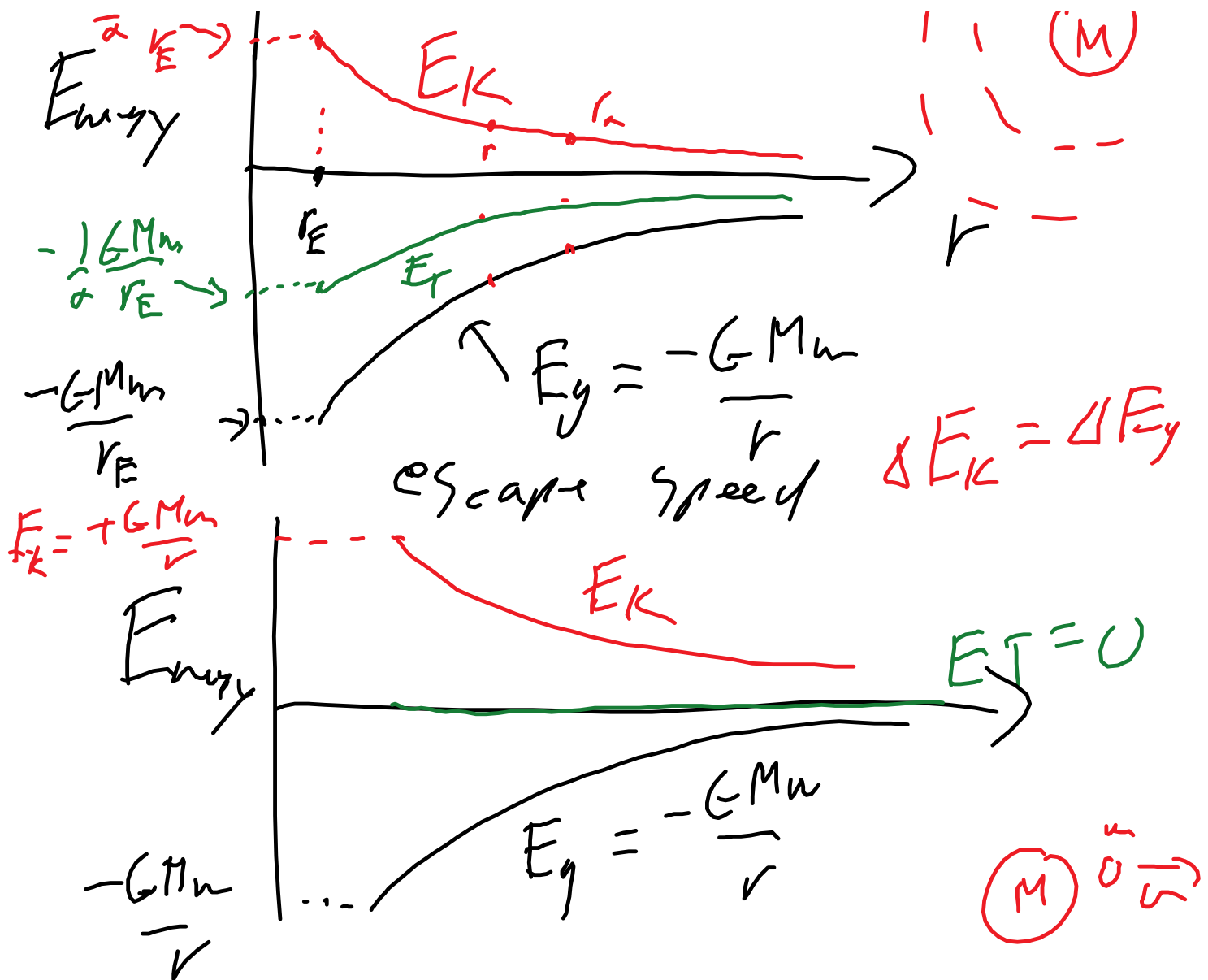
$$E_K = \frac{1}{2} m v^2 = \frac{1}{2} \left(\frac{GMm}{r} \right)$$

* orbital kinetic Energy $= \frac{1}{2} |E_g|$

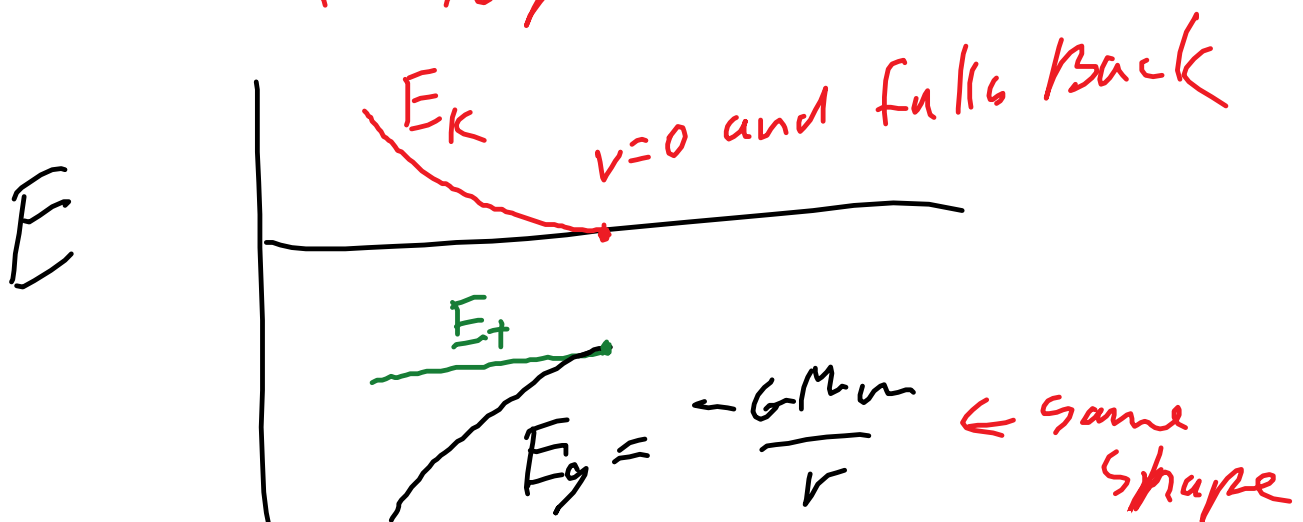
$$E_{\text{Total}} = E_K + E_g = \frac{1}{2} E_g$$

Orbital Energy Graphs





$V < V_{\text{escape}}$



$$V > V_{\text{escape}}$$

